

**12.25. Model:** Model the sun (s) and the earth (e) as spherical masses.

**Visualize:** The earth orbits the sun with velocity  $v_e$  in a circular path with a radius denoted by  $r_{s-e}$ . The sun's and the earth's masses are denoted by  $M_s$  and  $m_e$ .

**Solve:** The gravitational force provides the centripetal acceleration required for circular motion.

$$\frac{GM_s m_e}{r_{s-e}^2} = \frac{m_e v_e^2}{r_{s-e}} = \frac{m_e (2\pi r_{s-e})^2}{r_{s-e} T_e^2}$$
$$\Rightarrow M_s = \frac{4\pi^2 r_{s-e}^3}{GT_e^2} = \frac{4\pi^2 (1.50 \times 10^{11} \text{ m})^3}{(6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2)(365 \times 24 \times 3600 \text{ s})^2} = 2.01 \times 10^{30} \text{ kg}$$

**Assess:** The tabulated value is  $1.99 \times 10^{30} \text{ kg}$ . The slight difference can be ascribed to the fact that the earth's orbit isn't exactly circular.